

# Shell model analysis of intruder states and high-K isomers in the $fp$ shell

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**Abstract.** We perform a systematic shell-model study of collective intruder structures and fully aligned high-spin states in nuclei from the lower- $fp$  shell in the  $sdfp$  configuration space. We analyze the intruder structures associated with the 1p-1h cross-shell excitations from the  $sd$  shell that have been observed in several nuclei from this region, including  $^{44}\text{Ti}$  and  $^{44}\text{Sc}$ . We compare the shell-model calculations to the recent mean-field work (H. Zduńczuk, W. Satuła, R.A. Wyss, nucl-th/0408018) and experimental data (M. Lach, J. Styczeń, private communication). The high-spin behavior may be understood in terms of the competing cross-shell proton and neutron excitations. The interplay between proton and neutron intruder states is reflected in the angular-momentum dependence of electromagnetic rates.

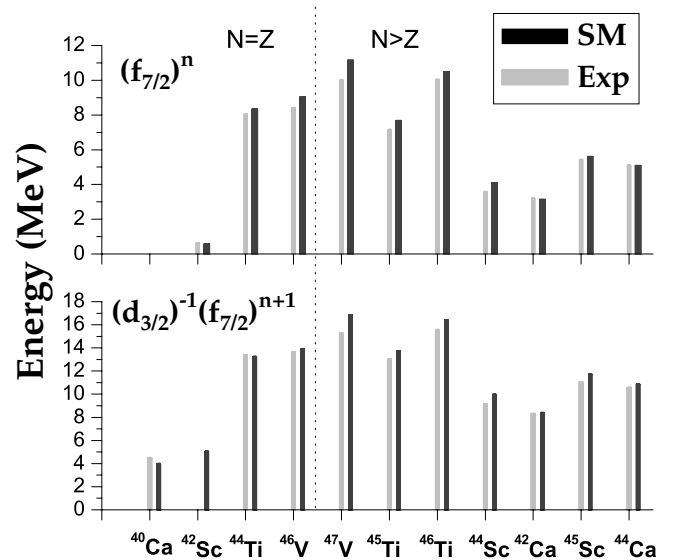
**PACS.** 21.60.Cs Shell model – 21.10.Ky Electromagnetic moments – 21.10.Pc Single-particle levels and strength functions – 27.40.+z  $39 \leq A \leq 58$

## 1 Introduction

The nuclei of the  $f_{7/2}$  shell are of special interest due to the presence of intruder states which can give rise to shape coexistence phenomena. These nuclei lie close to the doubly magic  $^{40}\text{Ca}$  and  $^{56}\text{Ni}$ , and therefore their structure can often be interpreted in terms of the competition between collective or single-particle excitations. One objective of this work is to analyze high-spin states of the lower- $fp$  shell nuclei based on large-scale shell-model (SM) calculations using the code ANTOINE [1]. In particular, we are interested in the intruder structures associated with cross-shell excitations across the  $N = Z = 20$  gap.

## 2 Shell model analysis

In this work, we study high-spin excitations in  $A \sim 44$ ,  $20 \leq Z \leq N \leq 24$  nuclei. An excellent agreement is observed between experiment and SM for the energies at the maximally aligned states of  $f_{7/2}^n$  (fig. 1, top) and  $d_{3/2}^{-1}f_{7/2}^{n+1}$  (fig. 1, bottom) structures. The black bars represent our SM calculations in which 1p-1h cross-shell excitations were allowed. They are compared to experimental data given by grey bars. We used the interaction of



**Fig. 1.** Comparison between SM and experiment for the maximum spin states in  $f_{7/2}^n$  (top) and  $d_{3/2}^{-1}f_{7/2}^{n+1}$  (bottom) configurations in several  $N = Z$  (left) and  $N > Z$  (right) nuclei in the  $fp$  shell.

ref. [2] where the mass scaling of the SM matrix elements was done consistently, thus reducing the  $sd$  interaction channel by  $\sim 4\%$  as compared to the previous work [2].

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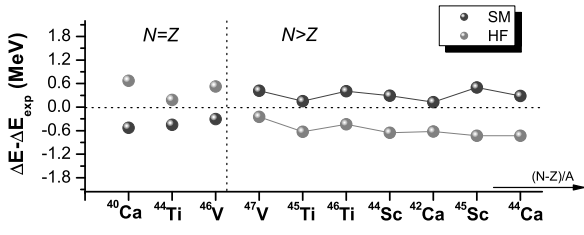


Fig. 2. Energy differences,  $\Delta E - \Delta E_{\text{exp}}$ , for SM and HF [3] calculations.

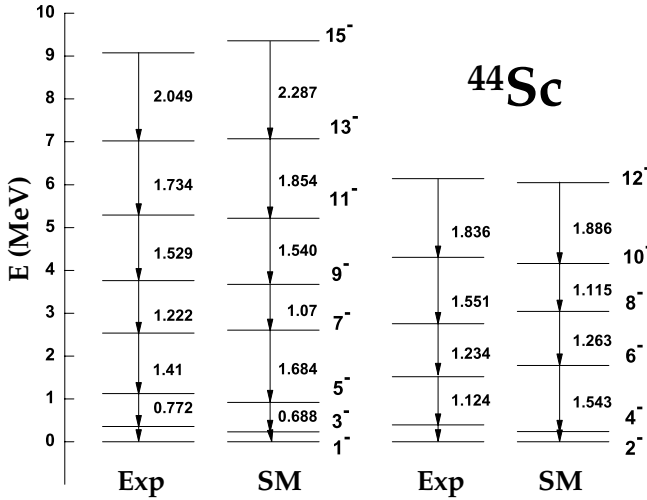


Fig. 3. Calculated negative-parity yrast structures in  $^{44}\text{Sc}$  compared to experimental data [4].

Figure 2 shows the SM and Skyrme Hartree-Fock (HF) [3] energy differences,  $\Delta E \equiv E(d_{3/2}^{-1}f_{7/2}^{n+1}) - E(f_{7/2}^n)$ , of the maximally aligned states, relative to experimental values. While for the  $N \neq Z$  nuclei, the SM calculations overestimate the data by  $\sim 10\%$ , HF underestimates them by  $\sim 10\%$ . However, it is interesting to see that the resulting energy difference patterns in the SM and HF are indeed very similar. In general, excellent agreement between the SM and experiment was obtained.

High-spin states of the odd-odd  $^{44}\text{Sc}$  nucleus have been studied in a recent experiment [4]. In the SM description, the positive-parity yrast structure of  $^{44}\text{Sc}$  has one proton and three neutrons in the  $f_{7/2}$  shell, and the maximum aligned state has  $I^\pi = 11^+$ . The negative-parity states up to  $I^\pi = 15^-$  can be associated with the holes in the  $sd$  shell.

A comparison between the experimental and calculated negative-parity band is given in fig. 3, while fig. 4 (bottom) shows the predicted  $B(E2)$  transition rates. The effective proton and neutron charges that are used in the calculations,  $e_p = 1.33e$  and  $e_n = 0.64e$ , have been determined from  $E2$  transitions in lower- $fp$  shell nuclei [5]. The transition rates and the shell occupations in the wave function (fig. 4, top) nicely show the interplay between proton and neutron intruder configurations for a given angular

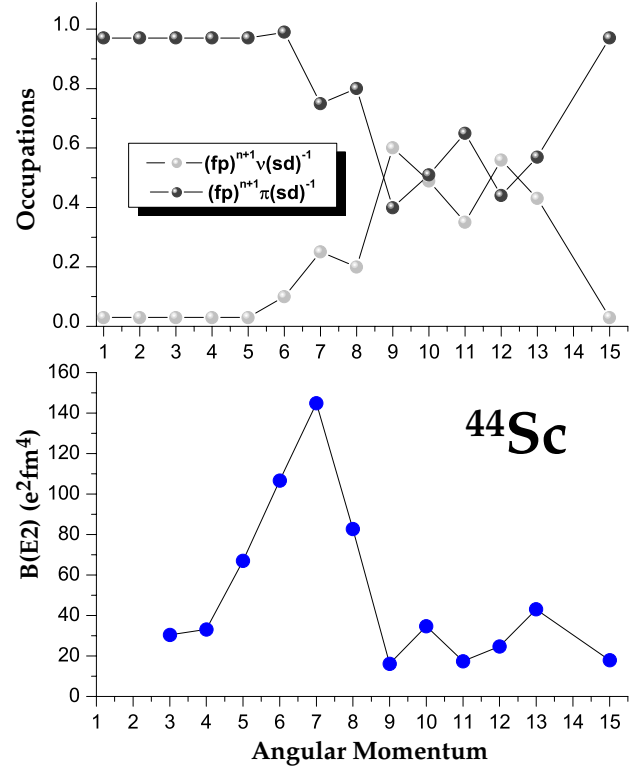


Fig. 4. Top: proton and neutron SM occupations in the  $\pi^-$  intruder structure of  $^{44}\text{Sc}$ . Bottom: calculated  $B(E2)$  rates within the intruder structure.

momentum  $I^\pi$ . It is predicted that the lower spin states as well as the highest  $I^\pi = 15^-$  spin state, are dominated by proton excitations. The intermediate angular-momentum spin states between  $I^\pi = 8^-$  up to  $I^\pi = 13^-$  are fairly equal mixtures of proton and neutron excitations.

As our present calculations are limited to 1p-1h cross-shell excitations only, some correlations are missing in our SM description. In particular, the structure  $N = Z$  nuclei can be affected by an explicit absence of the 2p-2h cross-shell  $T = 0$  excitations. This is shown in fig. 2, which clearly demonstrates a different behavior of  $\Delta E$  for  $N \neq Z$  and  $N = Z$  nuclei. Detailed studies of this effect are in progress [6].

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